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To what extent does hydrological connectivity control dynamics of faecal indicator organisms in streams? Initial hypothesis testing using a tracer-aided model

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Abstract

The role of hydrological connectivity in driving the dynamics of faecal indicator organisms (FIOs) in streams is poorly characterised. Here, we demonstrate how a tracer-aided hydrological model can be used within a coupled modelling approach to explore the role of connectivity in governing stream faecal coliform (FC) dynamics. To do so, we tested a hypothesis that in northern upland catchments, the dynamics of hydrological connectivity between major landscape units (hillslopes and riparian zone) and the stream exert a dominant control on stream FC loads by facilitating generation of runoff-driven FC fluxes. This hypothesis was conceptualised within a simple FC model that was coupled to a tracer-aided hydrological model developed for a small (3.2 km²) data-rich catchment in NE Scotland. The model was dual-calibrated to daily discharge and stable isotope data for the period August 2008 to September 2009; stream FC loads were also simulated but not used as a calibration target. Behavioural models successfully captured the general dynamics of the discharge and isotope data (average Kling-Gupta efficiencies of 0.72 and 0.53, respectively), providing confidence in the realism of simulated hydrological processes. The models simulated a seasonally-varying role of connectivity in driving stream FC loads. In summer, connectivity of the catchment hillslope was crucial in providing a source of FC to the riparian zone for transfer to the stream; this countered the decline in fresh FC input to the riparian zone in summer which reflected the seasonal movement of red deer (the principal source of FC) onto higher ground. In winter when this seasonal movement caused FC to be predominantly stored in the riparian zone, simulated hillslope connectivity primarily provided water to the riparian zone that permitted increased runoff generation and associated mobilisation of FC. Comparison of observed and simulated stream FC loads revealed model performance to be variable (R² range: 0-0.34). The better performance of the model in summer was consistent with hydrological connectivity being a dominant control on stream FC loads at this time. However, failure of the model to capture low FC loads in winter indicated that additional processes not considered in the model may also govern stream FC dynamics during this period. Incorporating the impact of freeze-thaw cycles on FC mortality, or a dilution effect of hillslope connectivity in winter, could be potential next steps in refining the hypothesis conceptualised in the FC model presented here. The novel coupled modelling approach used in this study successfully allowed a hypothesised role of connectivity in driving stream FC dynamics to be
tested, contextualised by the accuracy of discharge and isotope-tracer simulations as indicators of hydrological process realism. Therefore, coupling FIO and tracer-aided hydrological models has clear promise for furthering understanding of FIO dynamics, which is a vital precursor to the successful management of microbial water quality. Based on the experiences in this study, a “roadmap” for the future development and application of coupled approaches is also presented.

Key Words: Conceptual models; Faecal coliforms; Flow pathways; Microbial water quality; Stable isotope tracers; Upland catchments
1. Introduction

The extent to which spatio-temporal variations in hydrological connectivity govern the dynamics of faecal indicator organisms (FIOs) in streams represents a key area of research in relation to understanding microbial water quality (Oliver et al., 2016). FIOs, such as faecal coliforms (FC) and generic *E. coli*, are commonly used to indicate faecal contamination of waters, and thus the potential presence of faecal pathogens (Geldreich, 1996). Such pathogens, for example *E. coli* O157, can lead to gastrointestinal illness in humans if exposure occurs via consumption or recreational use of contaminated water (Fewtrell and Kay, 2015; Oliver et al., 2005). Whilst linkages between hydrological connectivity and faecal contamination have begun to receive attention in agricultural landscapes (e.g. Dorner et al., 2006; Muirhead and Monaghan, 2012; Porter et al., 2017), the issue has remained relatively unexplored in upland environments. This is despite a generally greater reliance on poorly-treated private drinking water supplies in such areas (Rodgers et al., 2003) and the role of headwater streams in influencing downstream water quality (Bishop et al., 2008; McDonnell and Beven, 2014).

Catchment-scale numerical models can be used as learning tools to further develop and refine process understanding (Dunn et al., 2008). In particular, testing different process-based model conceptualisations against observational data as competing hypotheses of catchment functioning, and informing future data collection needs through model application, has been advocated within the hydrological community (Beven, 2012; Clark et al., 2011; Gupta and Nearing, 2014). It has also been suggested that process-based models could be similarly used to address fundamental knowledge gaps in relation to the fate and transport of FIOs in catchments (de Brauwere et al., 2014; Oliver et al., 2016). Several such models that simulate both hydrological and FIO dynamics at the catchment scale already exist (e.g. Hipsey et al., 2008; Sadeghi and Arnold, 2002; Whitehead et al., 2016; Wilkinson et al., 2011). However, attempts to capture the many complex and often poorly-understood processes that are thought to affect the fate and transport of FIOs commonly result in highly-parameterised models that can be characterised by large degrees of uncertainty (Cho et al., 2016a; Porter et al., 2017). Furthermore, most existing FIO models only permit the adequacy of hydrological process representation to be
assessed based on how well the model can simulate discharge at the catchment outlet (Cho et al., 2016a).

However, discharge data alone cannot be used to assess how well the model represents internal catchment states and processes that strongly drive hydrological connectivity (Birkel et al., 2014; McDonnell and Beven, 2014). These limitations may, therefore, restrict many current FIO models in being used to understand the role of hydrological connectivity in driving stream FIO dynamics (c.f. Kirchner, 2006; Vache and McDonnell, 2006).

One route forward could be to explore modelling approaches that test hypotheses focused on identifying the dominant processes that underlie the complex dynamics often exhibited in catchment-scale empirical observations (Gupta and Nearing, 2014; McDonnell et al., 2007; Sivakumar, 2008). In a hydrological context, this approach has been particularly fruitful when applied in long-term experimental research catchments for which diverse datasets are available to inform process conceptualisation and aid in model testing (Tetzlaff et al., 2017). For example, the collection of long-term stable isotope and geochemical tracer data alongside traditional hydrometric data has allowed for the development of conceptual process-based tracer-aided models, which simultaneously simulate storage-driven water fluxes and their associated tracer concentrations (Birkel and Soulsby, 2015). Such models have led to substantial progress in the characterisation of flow paths, storage dynamics and connectivity for catchments in a wide range of environments, such as northern latitudes (McMillan et al., 2012; Smith et al., 2016; Tunaley et al., 2017), tropical regions (Birkel and Soulsby, 2016; Westerberg and Birkel, 2015) and karst landscapes (Zhang et al., 2017; 2018). This has largely been possible through the “grey box” approach adopted by such models, whereby perceptions of the dominant hydrological processes operating within a catchment are conceptualised within a parsimonious model structure (Birkel and Soulsby, 2015). Models are then evaluated based on their ability to simulate not only observed discharge data, but also to correctly capture the internal states and processes within a catchment that integrate to drive observed tracer dynamics at the catchment scale (Birkel et al., 2015; McDonnell and Beven, 2014). Through adopting a parsimonious approach, it is also possible for such models to be iteratively developed to test refined hypotheses of catchment
functioning as data availability and ideas about dominant processes evolve (Birkel and Soulsby, 2015; Dunn et al., 2008). Similar modelling approaches to test the dominant processes driving the dynamic FIO response of catchments have not yet been fully explored. This is despite it having been suggested that of the many factors thought to influence the fate and transport of FIOs (e.g. release kinetics, entrainment processes, streambed deposition and resuspension, and environmental factors such as pH and salinity affecting die-off [Cho et al., 2016a]), some, such as hydrological processes and temperature, may exert stronger controls (Kay et al., 2007; Tetzlaff et al., 2010; Bluestein et al., 2013).

Conceptual process-based tracer-aided models are not without their limitations. For example, there is a general need for calibration to the specific period of application and a necessary increase in parameterisation to allow for tracer simulation (Birkel and Soulsby, 2015). However, such models still have unrealised potential in providing greater confidence in the realism of simulated catchment hydrological functioning such that linkages between hydrological processes and water quality can be assessed (Birkel and Soulsby, 2015; Hrachowitz et al., 2016). In this work, we present a “proof-of-concept” in this regard with respect to microbial water quality. Specifically, we demonstrate how a tracer-aided model can provide a framework within which the role of hydrological connectivity in governing stream FC dynamics can be explored through a coupled modelling approach. The tracer-aided model employed in this study has been developed for the Bruntland Burn (BB) catchment in NE Scotland. The BB provides an ideal location for this study for two reasons. Firstly, the rich long-term hydrometric and tracer datasets collected for both the stream and spatially-distributed soil and groundwater monitoring locations, have been used to extensively inform and test the tracer-aided model structure (Birkel et al., 2010; 2014a; 2015; Soulsby et al., 2015). This has helped reinforce the consistency of the model with internal catchment processes (Birkel et al., 2014a), which in turn has offered confidence in its use to explore the hydrological drivers of water quality parameters such as dissolved organic carbon (Birkel et al., 2014b; Dick et al., 2015). Secondly, rapid rates of warming and changing precipitation patterns are expected to significantly impact water quantity and quality in northern upland environments such as the BB (Capell et al., 2013; Kundzewicz et al., 2007). Therefore,
understanding the drivers of faecal contamination in such landscapes is critical if future microbial water quality is to be maintained.

To provide the “proof-of-concept”, the specific aim of this study was to test a hypothesised role of hydrological connectivity in governing stream FC dynamics. In northern upland catchments, storage-driven connectivity between major landscape units (hillslopes and riparian zone) and the stream has been shown to be a dominant factor in driving the non-linear hydrological response characteristic of such environments (Soulsby et al., 2006; Spence and Woo, 2003; Tetzlaff et al., 2014). As such, we hypothesised that the dynamics of hydrological connectivity between landscape units and the stream also exert a dominant control on stream FC loads by facilitating generation of runoff-driven FC fluxes. Furthermore, we also suggest that groundwater makes a negligible contribution to stream FC, since near-surface and overland flow paths often dominate the hydrological response (Tetzlaff et al., 2010; Tyrell and Quinton, 2003), and that die-off of FC on the land surface is controlled by temperature (Bluestein et al., 2013). We conceptualised this hypothesis of catchment functioning within a simple FC model which we coupled to the tracer-aided hydrological model. The validity of the hypothesis was then tested through addressing the following objectives:

1. Use the model to spatially disaggregate sources and stores of water and FC to examine how hydrological connectivity between landscape units drives the simulated catchment-scale hydrological and FC responses.

2. Assess the performance of the model in simulating observed catchment-scale FC loads, contextualised by the accuracy of discharge and isotope-tracer simulations as indicators of hydrological process realism.

Based on our experience we also use the coupled model as a learning tool to suggest future improvements needed when combining FIO and tracer-aided hydrological models to better capture controls on stream FIO dynamics.
2. Study Site

The study was based at the BB (3.2 km²), a tributary of the long-term Girnock Burn research site (31 km²) in the Cairngorms National Park, NE of Scotland. The Girnock is a headwater of the River Dee, which is of great importance for conservation and as a regional drinking-water resource (Langan et al., 1997; Soulsby et al., 2016). The BB has a temperate / boreal oceanic climate. Mean annual air temperature is ~6 °C, ranging between 1 °C and 12 °C in winter and summer, respectively. On average, the BB receives ~1000mm of precipitation per year, which is generally evenly-distributed temporally in low-intensity rainfall events. Annual evapotranspiration averages ~400 mm.

The glacial legacy of the BB causes the catchment to have a wide, flat valley bottom surrounded by steeper hillslopes (Figure 1a). Furthermore, 70% of the catchment is overlain by glacial drift deposits. Previous hydrogeophysical work has indicated that this drift extends to depths of 5-10 m on the steeper hillslopes and up to 40 m in the valley bottom (Soulsby et al., 2016), and acts as a significant store and contributor of groundwater (Birkel et al., 2011b; Blumstock et al., 2015). Soils in the catchment form a classic catena sequence, grading from more freely-draining podzols and rankers on the steeper hillslopes to poorly drained peaty-gleys and peats (up to 4 m deep) in the valley bottom riparian zone (Figure 1b). The riparian zone remains close to saturation throughout the year, with the areal extent of saturation varying between 2% and 40% of total catchment area, depending on antecedent conditions (Figure 1a; Birkel et al., 2010). Saturation-excess overland flow from the riparian zone is the main source of runoff generated in response to precipitation events (Tetzlaff et al., 2014). However, the magnitude of the storm response is highly non-linear, depending strongly on hydrological connectivity between the steeper hillslopes and riparian zone (Soulsby et al., 2015). During wetter periods, expansion of the saturated area facilitates connectivity between these two parts of the catchment via lateral flow to produce the largest responses (Birkel et al., 2015). In drier conditions, however, the hillslopes can become disconnected from the riparian zone due to the predominance of vertical drainage that recharges groundwater (Blumstock et al., 2016; Tetzlaff et al., 2014). In the driest of conditions, baseflow in the stream is largely sustained by groundwater from the underlying drift deposits (Blumstock et al., 2015).
The hydrological functioning of the BB has been extensively studied and more details can be found in earlier work (e.g. Geris et al., 2015; Tetzlaff et al., 2014).

In the BB, high densities of red deer (*Cervus elaphus*) provide a key source of faecal contaminants, though contributions from smaller animals such as otters, water voles and mountain hares may also be possible (Tetzlaff et al., 2010). Results from a census of red deer densities in Scotland suggest densities in the BB could be as high as 11-14.9 deer km\(^{-2}\) (SNH, 2016), and excreted faecal material from deer is often clearly observable in the catchment. Generally, red deer in Scotland are more likely to occupy higher-elevation areas during summer, coming down into the valley bottoms during winter (Mitchell et al., 1977). However, the detailed movement of red deer is highly complex, varying on a range of timescales in different landscapes in response to various factors (Mitchell et al., 1977).

3. Data and Methods

3.1 Hydrometric, isotope and microbiological data

The study period was 12 August 2008 to 22 September 2009. Stream discharge was derived from stage measurements recorded at 15-minute intervals at the catchment outlet (Figure 1a) using an Odyssey capacitance logger (Odyssey by Dataflow Systems Pty Ltd, New Zealand) and an established rating curve. Meteorological data were primarily based on data collected by an automated weather station 1 km away operated by Marine Science Scotland, with daily average temperature being attitudinally corrected. Potential evapotranspiration (PET) was derived from these data using the Penman-Monteith equation (Allen et al., 1998). Catchment precipitation was interpolated using an inverse distance elevation gradient algorithm similar to Capell et al. (2012) based on five surrounding rain gauges.
maintained by the Scottish Environmental Protection Agency. All hydrometric data was aggregated into a daily dataset.

ISCO 3700 autosamplers were used to collect stream water spot samples at the catchment outlet (Figure 1a) and bulk precipitation samples at daily intervals for stable isotope analysis. A layer of paraffin was added to bottles used to collect samples for isotope analysis to prevent evaporation. Samples were analysed for deuterium ($\delta^2$H) and oxygen-18 ($\delta^{18}$O) using a Los Gatos DLT-100 laser isotope analyser (precision of ±0.4‰ for $\delta^2$H and 0.1‰ for $\delta^{18}$O). Isotope data are expressed in δ-notation with respect to the Vienna Standard Mean Ocean Water. Given the higher relative precision of $\delta^2$H, these data were used for modelling purposes.

Stream water samples were also collected at approximately weekly intervals for FC analysis. Samples were collected in sterilised bottles, with the standard membrane filtration method using mFC agar plates incubated at 44 °C for at least 18 h (APHA, 1992) adopted to determine concentrations of FC, in colony forming units (CFU) 100 ml$^{-1}$, within 3-4 hours of sample collection. In all cases, an undiluted sample of 100 ml was filtered, with additional dilutions filtered if samples were suspected to be highly contaminated. As such, the limit of detection for FC was 1 CFU 100 ml$^{-1}$ (approximate 95% confidence intervals for colony counts greater than 20 for 100 ml sample: $\text{count} \pm 2\text{count}^{0.5}$; otherwise see Table 9222:II in APHA, 1992). FC loads (in CFU day$^{-1}$) were calculated for the catchment outlet by multiplying concentrations by average daily discharges (converted to units of 100 ml day$^{-1}$). When concentrations were below the limit of detection, an upper limit to the FC load was calculated using a concentration of 1 CFU 100 ml$^{-1}$.

3.2 Tracer-aided hydrological model
The tracer-aided hydrological model used has been developed for the BB based on extensive empirical and modelling studies (Birkel et al., 2010; 2015; Soulsby et al., 2015). The reader is referred to these papers for details and only a brief overview follows. The model captures the non-linear hydrological response of the BB by conceptualising the hydrological connectivity between three distinct hydrological stores representing the major landscape units (Figure 2a). The dynamic hillslope and dynamic riparian zone broadly represent the more freely-draining podzols of the hillslopes and the saturation-prone peaty soils of the valley bottom, respectively. There is also a groundwater store. The expansion and contraction of the areal extent of saturation is represented by a model input, $d_{Sat}$, which is a daily time series generated by an antecedent precipitation index-type algorithm that describes the daily extent of saturation in the catchment (Birkel et al., 2010). The value of $d_{Sat}$ on any day is used to distribute daily time series of precipitation ($P$) and PET between the dynamic hillslope ($P_{up}, PET_{up}$) and riparian zone ($P_{sat}, PET_{sat}$), which contribute to or deplete the dynamic storages ($S_{up}$ and $S_{sat}$, both in mm) of each store (Figure 2a).

To capture storage-driven threshold processes of runoff generation in the BB (Tetzlaff et al., 2014), the dynamic storages of each hydrological source area are permitted to go into deficit; these have to be filled before runoff can be generated (Birkel et al., 2015). The dynamic hillslope can drain into the dynamic riparian zone (flux $Q_{up}$, in mm day$^{-1}$) and recharge the groundwater reservoir (flux $R$, in mm day$^{-1}$). Both fluxes are linear functions of $S_{up}$ and are controlled by the rate parameters $a$ and $r$ (in day$^{-1}$), respectively. Flux $Q_{sat}$ (in mm day$^{-1}$) is a power function of $S_{sat}$ controlled by the rate parameters $k$ (in units of day$^{-1}$) and $\alpha$ (dimensionless), and conceptualises the non-linear generation of saturation excess overland flow from the riparian zone to the stream. Streamflow ($Q_{stream}$, in mm day$^{-1}$) is the sum of $Q_{sat}$ and $Q_{low}$ (in mm day$^{-1}$), the latter being a groundwater flux that is a linear function of groundwater storage ($S_{low}$, in mm) controlled by the rate parameter $b$ (in day$^{-1}$).
The isotopic composition of water in each hydrological store evolves based on the following equation:

\[
\frac{d(c_S)}{dt} = \sum_j c_{I,j}I_j - \sum_k c_{O,k}O_k \quad \text{(Eq. 1)}
\]

where \( c \) is the \( \delta^2H \) composition (‰) of \( j \) storage inflows \( I_j \) (e.g. P, \( Q_{up} \), R) and \( k \) outflows \( O_k \) (e.g. \( Q_{low} \), \( Q_{sat} \)) causing changes in the storage \( S \) of a hydrological store with isotopic composition \( c \). As each store is assumed to be well mixed, the isotopic compositions of any outflow is equal to the composition of the store from which it came. For the isotope transport simulations, the storage \( S \) includes both the dynamic storage and an additional mixing volume (MV) that does not contribute to runoff generation (Figure 2a). The MVs are dynamic in time, arising from calibrated storage parameters for each store (\( upS_p \), \( lowS_p \), \( satS_p \) in mm) that are converted to daily MVs based on the value of \( dSat \). In wetter conditions when \( dSat \) is larger, the expansion of the saturated riparian area causes greater potential for mixing in this part of the catchment at the expense of mixing on the hillslopes (Figure 2a). By dynamically varying the mixing that takes place in the riparian zone and hillslope stores, the complete mixing of the individual storages is integrated at the catchment scale in a non-linear manner, thus resulting in a partial mixing mechanism. The additional mixing volumes are required to capture the importance of large storage volumes that are necessary to damp the isotopic signature of streamflow with respect to precipitation, as shown in previous work (Birkel et al., 2011a; Soulsby et al., 2015).

Previous work in the BB showed that evaporative isotopic fractionation is an important process changing isotopic compositions, particularly in the riparian zone where the fractionated isotopic signal can be translated to stream water (Sprenger et al., 2017). As such, fractionation was accounted for in the dynamic riparian zone of the model using the following equation, based on Benettin et al. (2017, Appendix B):
which conceptualises the change in the isotopic composition of riparian zone storage ($\delta^2H_{sat}$ in ‰) at time $t$ as a function of an isotopic depletion factor ($\alpha_{ET}$), actual evapotranspiration ($AET_{sat}$, in mm) from the riparian zone, total storage in the riparian zone ($S_{sat} + satMV$) and the isotopic composition of the riparian zone, at time $t$. The term $\alpha_{ET}$ requires calibration, and can vary between 0 and 1. A value of 1 indicates no fractionation (Benettin et al., 2017). Eq. 2 is used to directly provide an enrichment amount ($frac_{sat}$ in Figure 2a) that is added to the simulated isotopic composition of the riparian zone storage at each timestep to account for evaporative fractionation.

3.3 Faecal coliform model

Since we suggest that FC contributions from groundwater will be negligible, the FC model considers only two stores of FC: the dynamic hillslope and dynamic riparian zone (Figure 2b). To be consistent with trying to adopt a modelling approach that refrains from trying to conceptualise all the complex processes relating to FIOs, we adopt a simple loading function for FC that attempts to capture just the seasonal movements of red deer (assumed to be the major source of FC in the BB). At each time-step, the presence of deer in the catchment is randomly determined. If deer are present, uniform random sampling is used to determine a total number of deer in the catchment between 1 and 50 – the upper limit reflects the upper deer density of 14.9 deer km$^{-2}$ reported for the BB by SNH (2016). A sinusoidal function describing the probability of deer being in the riparian zone is then used to distribute the total number of deer between the hillslope and riparian zone. The function is at its minimum at the beginning of July, and its maximum at the end of December / beginning of January. As such, deer are most likely to be found on the hillslope at the height of summer and in the riparian zone during winter (Mitchell et al., 1977). FC loading by deer to each store is then calculated by multiplying the number of deer by
daily FC excretion per deer. Uniform random sampling is used to determine the FC excreted per deer at each time step to reflect the fact that this is unlikely to be consistent in time and to account for uncertainty in reported excretion of FC by deer (Oliver et al., 2010). To the authors’ knowledge, the latter has not been extensively investigated, with only a single value of $5 \times 10^8$ CFU deer$^{-1}$ day$^{-1}$ for deer in the Lower Mississippi River Basin (Senjem et al., 2002) being found after a literature review. The range from which daily FC excretion was sampled was $\pm 1$ order of magnitude from this value as a reasonable uncertainty bound (Oliver et al., 2010).

Die-off of FC in storage is modelled based on first-order kinetics using Chick’s Law (Chick, 1908):

\begin{equation}
 C = C_0 e^{-kt}
\end{equation}

(Eq. 3)

where $C$ is number of bacteria, $C_0$ is the starting number of bacteria, $k$ is an inactivation rate constant (in units day$^{-1}$) and $t$ is time since $t_0$. The inactivation rate constant for FC in storage was calculated as a function of temperature using the following equation based on the Arrhenius equation:

\begin{equation}
 k_{\text{deer}}(t) = k_0 \theta(T(t) - T_0)
\end{equation}

(Eq. 4)

where $k_{\text{deer}}(t)$ is the inactivation rate constant (in units of day$^{-1}$) for FC excreted by deer at time $t$, $k_0$ is the inactivation rate constant (in units of day$^{-1}$) at a reference temperature ($T_0$) set here to 20 °C, $\theta$ is a temperature sensitivity parameter (dimensionless), and $T(t)$ is air temperature (in units of °C) at time $t$. Since a literature review did not yield specific values of $k_0$ and $\theta$ for FC from red deer, values for $E. coli$ excreted by white-tailed deer of 0.175 day$^{-1}$ and 1.007 were used for each parameter, respectively.
Since the values of $k_0$ and $\theta$ can be highly dependent on the host animal, it is likely that these values will be more representative for red deer than values specifically for FC but from other animal groups (Guber et al., 2015).

Accounting for inputs of FC (which for the riparian zone also includes inputs from the hillslope – see below) and die-off of FC already in storage, the FC available at time $t$ for mobilisation from either the dynamic hillslope or riparian zone is described by:

$$FC(t) = FC_{in}(t) + FC(t - 1)e^{-k_{deer}(t)}$$

(Eq. 5)

where $FC(t)$ is FC in storage (in CFU) at time $t$, $FC_{in}(t)$ is inputs of FC (in CFU) at time $t$, and the final term in the equation is FC in storage (in CFU) at time $(t-1)$ subjected to die-off following Chick’s Law with a temperature-dependent inactivation rate constant. To conceptualise the mobilisation and transport of FC as a function of runoff generation, fluxes of FC ($upFC\_Flux$ and $satFC\_Flux$, in CFU day$^{-1}$) are modelled in a similar manner to that of Wilkinson et al. (2011), whereby the proportion of FC stored in either the dynamic hillslope ($upFC$, in CFU) or riparian zone ($satFC$, in CFU) stores that is flushed out with runoff is equal to the proportion that the simulated runoff from either store ($Q_{up}$ or $Q_{sat}$) is of the maximum observed stream discharge for the study period (Figure 2b). This has physical meaning, as the ability of runoff to transport FC will likely depend on its depth and velocity, as this will determine how effectively the flow can entrain and suspend FC that are either free microorganisms or attached to faeces (Tyrell and Quinton, 2003). Fluxes of FC from the hillslope contribute to the FC that is able to be mobilised from the riparian zone, whilst the simulated stream FC load (in CFU day$^{-1}$) is simply the FC that is flushed from the riparian zone store (Figure 2b). Given the small channel characteristics of the BB and the high velocity of steep upland streams, we do not consider a channel.
store of FC, nor is further die-off of FC in the stream water column considered as it is transported to the catchment outlet.

3.4 Model application

The model was applied with a daily time step and was calibrated for the study period. However, data for the preceding three years were used as spin-up to initialise the model. In total, the coupled model had nine parameters, relating to hydrological and tracer simulation, that required calibration. Calibration was achieved by conducting 5,000,000 Monte Carlo simulations with parameter values drawn randomly from uniform distributions with upper and lower bounds informed by previous applications of the tracer-aided model (Table 1; Birkel et al., 2010; 2015). Behavioural parameter sets were identified as those which simultaneously achieved modified Kling-Gupta efficiencies (KGEs) of ≥ 0.7 and ≥ 0.5 for discharge and isotope-tracer simulations, respectively. A lower threshold for isotope simulations was used since it was expected that the model may not be able to capture the complex shorter-timescale variability in the observed data, but instead reflect the more medium- to longer-term trends (e.g. Page et al., 2007). The modified KGE (Kling et al., 2012) is given by:

\[
KGE = 1 - \frac{1}{\sqrt{(r_{cor} - 1)^2 + (\beta - 1)^2 + (\gamma - 1)^2}}
\]

(Eq. 6)

where \(r_{cor}\) is the correlation coefficient between simulated and observed values, \(\beta\) is the mean of simulated values divided by the mean of observed values (bias ratio) and \(\gamma\) is the coefficient of variation of simulated values divided by the coefficient of variation of observed values (variability ratio). To better assess the physical realism of the proposed dominant processes driving stream FC conceptualised within the coupled model, observed FC loads were not used as part of model calibration (c.f. Kuppel et al., 2018). However, an \(R^2\) value was calculated to describe the ability of the model to simulate the observed loads. This metric was chosen to focus on the skill of the model in simulating the timing and
variance, rather than the magnitude, of the observed FC loads, since the ability to capture the latter
could potentially be impacted by uncertainties in the input data relating to FC simulations. To account
for uncertainty in the magnitude of FC loads when stream FC concentrations were below the limit of
detection, two sets of $R^2$ values were calculated assuming for these periods that either 1) all FC loads
were zero, or 2) all FC loads were at their upper limit.

[Table 1]

Behavioural parameter sets were retained for simulation of stores and fluxes of water and FC within the
catchment, as well as of stream discharge, tracer and FC dynamics. To permit spatial disaggregation of
sources and stores of water and FC, the median values of simulated outputs from all behavioural models
were taken to represent an average simulation. These values were used to assess the contribution made
at each model timestep (instantaneous contribution) by inputs of either water or FC from the hillslope
to the total store of water or FC in the riparian zone available for either the generation of
evapotranspiration and runoff, or FC fluxes to the stream, during that same timestep:

$$Perc_{Hill}(t) = \frac{Flux_{Hill}(t)}{Input_{Rip}(t) + Flux_{Hill}(t) + Storage_{Rip}(t-1)} \times 100$$  \hspace{1cm} (Eq. 7)

Here, $Perc_{Hill}(t)$ is the contribution (in %) that hillslope fluxes of either water or FC generated at time $t$,
$Flux_{Hill}(t)$, make to the total store of water or FC available in the riparian zone for hydrological or FC
flux generation at time $t$. The total store available is defined as the store of water or FC in the riparian
zone at the end of the last timestep, $Storage_{Rip}(t-1)$, plus inputs from the hillslope, as well as any direct
inputs (i.e. precipitation or defecated FC) to the riparian zone, $Input_{Rip}(t)$, at time $t$. Die-off at time $t$ of
FC already stored in the riparian zone at time $t-1$ is accounted for prior to application of Eq. 7. The
percentages of total FC in the BB (\textit{upFC} + \textit{satFC}) stored in either the dynamic hillslope or dynamic riparian zone at the end of each timestep after accounting for FC fluxes were also assessed. For simulation of the stream dynamics, the median and 90\% spread (5\textsuperscript{th} to 95\textsuperscript{th} percentile) of outputs simulated by the behavioural models were used as an indication of uncertainty arising from variability in parameter values.

4. Results

4.1 Hydroclimatic, isotope and microbiological dynamics

Hydroclimatic conditions during the study period were typical for the region, generally being characterised by low-intensity precipitation events (< 10 mm day\textsuperscript{-1}) that exhibited limited seasonality, and to which discharge often showed a clear response (Figure 3a). The largest precipitation event occurred in February 2009 (65 mm day\textsuperscript{-1}), which also resulted in the highest observed mean daily discharge of 14.24 mm day\textsuperscript{-1}. Periods of more limited precipitation and predominantly baseflow conditions in the stream were observed for April to early May, and during the latter part of September 2009. During winter, mean daily temperatures could fall to -9.7 \degree C, whilst in summer temperatures peaked at 20.7 \degree C (Figure 3b). PET varied seasonally between 0 and 2.6 mm day\textsuperscript{-1} (Figure 3b).

The \textit{\delta}H of stream water was damped compared to precipitation (Figure 3c), with the former ranging between -72.2\%o and -49.2\%o and the latter between -167.2\%o and -2.3\%o. This reflects mixing of incoming precipitation with pre-event water stored in the catchment. However, during larger events where there was a clear discharge response, the precipitation \textit{\delta}H signal became more apparent in the stream \textit{\delta}H signal. Gaps in the stream isotope data between January and March 2009 arose from autosampler failure.
Concentrations of FC varied over three orders of magnitude (Figure 3d). Concentrations exhibited marked seasonality, being highest during summer (maximum of $3.4 \log_{10} \text{CFU 100 ml}^{-1}$ in August 2008). In winter, meanwhile, concentrations could be below the limit of detection for prolonged periods (e.g. two five-week periods between January and March 2009). A clear response of concentrations of FC to discharge was generally not apparent, although higher-discharge events during summer months were generally associated with elevated concentrations. Calculated FC loads displayed similar temporal dynamics to concentrations, with the peak load of $11.2 \log_{10} \text{CFU day}^{-1}$ corresponding to the peak concentration (Figure 3d). When FC concentrations were detectable, FC loads varied over approximately four orders of magnitude. The upper limits calculated for FC loads when concentrations were below the limit of detection did not exceed $7.9 \log_{10} \text{CFU day}^{-1}$.

4.2 Model calibration

Of the 5,000,000 initial parameter sets, 34,853 satisfied the criteria to be considered behavioural of simultaneously achieving KGEs of $\geq 0.7$ and $\geq 0.5$ for discharge and isotope-tracer simulations, respectively. The 90% spread ($5^{\text{th}}$ to $95^{\text{th}}$ percentile) of behavioural values for each parameter generally extended across much of the respective initial sampling ranges (Table 1). Exceptions were values for the parameters $upS_p$, $satS_p$, and, to some extent, $\alpha$. Both $upS_p$ and $satS_p$, in particular, tended to favour values in the lower part of their respective initial sampling ranges. Therefore, for isotope transport simulation, MVs and hence the potential for mixing was, on average, greatest in groundwater and lowest in the riparian zone ($lowS_p > upS_p > satS_p$). The tendency for $\alpha$ to not have behavioural values at the lower end of the initial sampling range, meanwhile, indicated a preference for more non-linear runoff generation from the riparian zone.

4.3 Spatial disaggregation of sources and stores of water and faecal coliforms
To examine how hydrological connectivity between landscape units drives simulated catchment-scale hydrological and FC dynamics, sources and stores of water and FC within the BB were spatially disaggregated (Figure 4). The importance of hydrological connectivity between the dynamic hillslope and riparian zone in the simulation of non-linear discharge responses at the catchment outlet is apparent from Figure 4b. Hillslope connectivity was induced by most precipitation events, suggesting that hillslope storage deficits were generally quite low. When connected, the peak instantaneous contribution of water from the hillslope to the riparian zone for individual periods of connectivity averaged 34%. This average was representative of periods of connectivity throughout the study period – i.e. contributions did not show a clear seasonal dynamic. The overall maximum contribution of 73% occurred in response to the February 2009 precipitation event. During periods of limited rainfall (e.g. April to early May 2009) when the hillslope was disconnected, sufficient water remained in the riparian zone to generate runoff to the stream; however, groundwater was increasingly responsible for sustaining stream discharge (Figure 4b).

Unlike contributions of water from the hillslope, instantaneous contributions of FC from the hillslope to the riparian zone showed strong seasonality (Figure 4c). The largest contributions of FC from the hillslope were during May to September, with peak contributions for individual connectivity events averaging 40%, and the maximum contribution of 97% occurring in mid-July 2009. By contrast, peak contributions for individual connectivity events during the remaining months averaged only 7%. This seasonality in contributions of FC, but not of water, from the hillslope arose from the clear seasonal pattern in the distribution of FC stored in the catchment between the hillslope and riparian zone (Figure 4d), which reflected the movement of red deer encapsulated within the FC loading function of the model. Throughout the study period, the simulated total FC stored in the BB was quite stable (average of $11.1 \log_{10}$ CFU), except following flushing of larger amounts of FC during the two largest discharge events.
events in December 2008 and February 2009. However, the percentage of the FC stored in the riparian zone (hillslope) clearly varied between a maximum (minimum) at the beginning of January and a minimum (maximum) at the beginning of July following a generally sinusoidal pattern. Deviations from this pattern arose when connectivity of the hillslope caused FC to be flushed to the riparian zone to increase the share of the total FC stored in the latter.

The influence of the spatial distribution of stored FC on the ability of the hillslope to contribute FC to the riparian zone meant that hydrological connectivity had a seasonally-varying role in driving simulated stream FC dynamics of the BB. During the months of October to April, connectivity between the hillslope and riparian zone primarily resulted in increases in stream FC load by causing greater amounts of runoff to be generated from the riparian zone which could mobilise the larger amounts of FC stored in this part of the catchment during these months (Figure 4b-d). Patterns of variability in simulated FC loads during this period generally reflected the patterns of variability in the simulated stream discharge. During the months of May to September, however, connectivity of the hillslope also became important in providing FC to the riparian zone that could be used for the generation of FC fluxes to the stream, to counter the general decline in the proportion of the total FC stored in the riparian zone which reflected the movements of red deer. As a result, stream FC loads during this period showed much greater variability than during October to April, with FC loads peaking in response to the hillslope becoming connected to the riparian zone, but then declining rapidly following disconnection as the generation of FC fluxes from the riparian zone to the stream became increasingly supply-limited.

4.4 Simulation of discharge, isotope and FC-load dynamics at the catchment scale

In order to test the validity of the hypothesised dominant controls on FC dynamics conceptualised within the coupled model and, thus, also gain some perspective on the likely physical representativeness of the simulated sources and stores of water and FC described in Section 4.3, the ability of the model
to simulate observed catchment-scale FC loads was assessed, contextualised within the performance of
the model in relation to simulating observed discharge and isotope-tracer dynamics.

The average and maximum KGEs achieved by the behavioural models for discharge simulations were
0.72 and 0.86, respectively. Event dynamics and magnitudes of observed discharge peaks were
generally well-captured by the behavioural models (Figure 5a); however, it was sometimes the case that
subtleties in the observed discharge data were not well-simulated by the models. For example, the
behavioural models at times under-estimated the flashiness of the discharge response, with the falling
limb of some events (e.g. events in September to November 2008 and the February 2009 peak discharge
event) simulated to be more prolonged than was observed in reality. In addition, the ability of the models
to capture small observed discharge responses was sometimes inconsistent, with the models over-
estimating the small discharge response that occurred in mid-October 2008, and under-estimating two
small discharge responses that occurred in mid-July 2009. Periods of low flow, such as April to mid-
May 2008, also tended to be slightly under-estimated.

Variations in the stream water isotope signal were captured reasonably well, with average and
maximum KGEs of 0.53 and 0.62 achieved by the behavioural models, respectively. The models
successfully reproduced the damped signal of the stream with respect to precipitation (Figure 5b), and
also captured the summer enrichment of the stream isotope signal more successfully than previous
applications of the model (e.g. Birkel et al., 2014; Soulsby et al., 2015). The overall skill of the model
in simulating the observed isotope signal was probably linked to an extent to the accuracy of discharge
simulations. For example, deviations between the observed and simulated isotope signal during
September to November 2008 may reflect the limitations of the model in simulating stream discharge
during this period. In other instances where discharge simulations were more accurate, deviations
between observed and simulated isotopes may have reflected incorrect relative contributions of riparian
zone runoff and groundwater to stream discharge. For example, at the end of June 2009, the behavioural
models simulated isotope values that were too enriched relative to observations, which may reflect the models translating too much of the enriched precipitation signal at that time (Figure 3c) to the stream via riparian zone runoff, at the expense of contributions of groundwater that typically has a more depleted isotopic composition (Soulsby et al., 2015). It should be noted, however, that deviations between observed and modelled stream isotopes were only on the order of a few per mille, with the general directions of variability in the observed isotope dataset being captured quite well.

[Figure 5]

The ability of the behavioural models to simulate observed FC loads was variable (Figure 5c), with values of $R^2$ ranging from 0 to 0.34 across both sets of calculated values. Model performance was best in the summer months, with uncertainty bounds (arising from uncertainty in the tracer-aided hydrological component of the model and the random component of the FC loading function) encompassing some observed FC loads, and also capturing some of the observed dynamics. The main failure of the behavioural models was their inability to capture the seasonality of observed FC loads (Figure 3d). The key period of model failure was January to March 2009. Here, simulated FC loads consistently exceeded the upper limits for observed loads that were calculated for the prolonged periods when FC concentrations were below the limit of detection. Some of the more minor deviations between observed and simulated FC loads probably reflected limitations in the tracer-aided component of the model in capturing some of the subtleties in the observed discharge and isotope data highlighted previously. For example, the over-estimation of FC loads in the latter part of 2008 was likely to have arisen from discharge often being over-estimated in this period, whilst the under-estimation of FC loads in July 2009 may be a consequence of the models not simulating the small discharge events that were observed. In addition, the failure of the models to capture isolated occurrences of lower FC loads may reflect simulation of runoff generation from the riparian zone to the stream when in actuality groundwater was the main contributor to discharge (e.g. at the end of June 2009).
5. Discussion

5.1 Exploring the role of hydrological connectivity in driving catchment-scale FC dynamics with a coupled tracer-aided model

Many process-based FIO models can be impacted by high degrees of parametrisation and uncertainty, and model structures that limit assessment of hydrological process realism and internal catchment states (Cho et al., 2016a; Hrachowitz et al., 2016). This hinders their application in exploring hypotheses that could address fundamental knowledge gaps surrounding the fate and transport of FIOs, including the role that hydrological connectivity plays in governing stream FIO dynamics. (Oliver et al., 2016). Here, the novel coupling of a parsimonious tracer-aided hydrological model and simple FC model has allowed a hypothesised role of hydrological connectivity in governing stream FC dynamics to be tested within the context of the inferred realism of simulated hydrological processes and internal catchment states.

The skill of the hydrological component of the model in simulating the general dynamics of both the observed discharge and tracer responses of the BB (Figure 5a-b) gives reassurance that the hydrological functioning of the catchment is being captured with reasonable accuracy such that the hypothesised role of connectivity in driving stream FC dynamics can be assessed (c.f. McDonnell and Beven, 2014; Vache and McDonnell, 2006). The performance of the coupled model in simulating observed FC loads strongly suggests that hydrological connectivity between landscape units and the stream exhibits an important control on stream FC dynamics through facilitating runoff-driven FC fluxes, at least during certain times of the year (Figure 5c). In particular, an important inference from the modelling was the crucial role of hillslope connectivity in providing FC to the riparian zone during the summer months (Figure 4c-d). When connectivity was established, elevated stream FC loads were simulated that opposed the general decreasing trend in simulated loads over the summer, reflecting the seasonal movement of red deer to the hillslope and the associated reduction of FC stored in the riparian zone (Figure 4d). This allowed some observed FC loads during this period to be bracketed by simulations (Figure 5c), and suggests
that, during the summer months at least, hydrological connectivity between the hillslope and riparian zone can drive non-linearities in stream FC load dynamics. This would be consistent with the importance of connectivity between the hillslope and the riparian zone in driving non-linearities in the hydrological response of northern upland catchments (Figure 4b; Birkel et al., 2015; Tetzlaff et al., 2014; Wells et al., 2017), and in other water quality parameters such as dissolved organic carbon (e.g. Dick et al., 2015).

The failure of the model to capture the seasonality in observed FC loads, however, indicates that the current hypotheses of system functioning conceptualised within the model are insufficient to fully identify the dominant processes driving stream FC dynamics in the BB (c.f. Beven, 2012; Dunn et al., 2008). Since the model continued to capture the general dynamics of the observed discharge and tracer data during the winter (Figures 5a-b), the failure in simulating observed FC loads during this period suggests that it is the hypothesis relating to the processes governing FC production and distribution in the catchment, rather than hydrological functioning, that needs refinement. This is further supported by the wealth of data on which the tracer-aided component of the model is based and its past successes in simulating biogeochemical parameters such as dissolved organic carbon which have a less-complex seasonal dynamic (Birkel et al., 2014a; 2014b; Dick et al., 2015). It is important to note that, to some extent, the well-known need for improved estimates of FIO die-off and loading parameters for wild animals and the resultant uncertainty in the values of these parameters used for red deer in this study are likely to have impacted on FC simulations (c.f. de Brauwere et al., 2014; Guber et al., 2015; Oliver et al., 2016). However, given that the period of significant model failure is restricted to the winter months, it is likely that the hypothesis conceptualised in the FC component of the model may be missing dominant processes affecting FC dynamics during this period.

If it is correct that connectivity exerts a major control on stream FC dynamics through facilitating runoff-driven FC fluxes, the period of model failure would suggest the absence of a process that reduces
the store of FC available for transfer to the stream in winter, instead of it remaining fairly stable (Figure 4d). Substantial increases in bacteria mortality can occur in response to repeated freeze-thaw cycles (Habteselassie et al., 2008; Natvig et al., 2002). Given the climate in northern upland environments like the BB (Figure 3b), freeze-thaw cycles over winter are common. Dawson et al. (2011) identified that the 42-day antecedent mean temperature is a useful predictor for defining the switchover between summer/autumn and winter/spring biological processes in NE Scotland. If a value for this variable of 2 °C or less is taken as indicative of when diurnal temperature fluctuations may have allowed freeze-thaw cycles to occur, it can be shown that a substantial part of the key period of model failure between January and March 2009 may have been impacted by increased FC mortality (blue shaded area in Figure 5c). As such, one potential refinement to the hypothesis conceptualised within the FC component of the model could be to allow for increased FC mortality in response to repeated freeze-thaw cycles, to determine whether this would permit more successful simulation of winter FC loads. To achieve this, however, would also require efforts to better characterise the non-linearities in inactivation rate constants caused by processes such as freeze-thaw, especially with respect to FIOs from wild animals (c.f. Crane and Moore, 1986; Guber et al., 2015).

It may also be necessary, however, to consider alternative roles of connectivity in winter to enable the model to capture the lower FC loads. One possibility could be to investigate whether higher influxes of less-contaminated hillslope water dilute FC concentrations in the riparian zone, leading to lower concentrations and loads being observed in the stream. Such a mechanism would be consistent with the riparian zone often being identified as a critical mixing zone which integrates the characteristics of different source waters in a catchment to set stream water quality (Seibert et al., 2009; Tetzlaff et al., 2014; Tunaley et al., 2016). In summer, a riparian dilution effect on more-contaminated influxes of water from the hillslope would be expected to be less pronounced, as a store of FC is maintained in the riparian zone even in the absence of fresh inputs from red deer due to influxes of FC from the hillslope. Testing this new conceptualisation of connectivity would require the model to be modified to deal with
concentrations of FC as well as loads so that increased runoff generation could lead to dilution as well as greater mobilisation of FC.

In addition to the most notable poor performance of the model in winter, there were also other deviations between observed and simulated FC loads, such as in late 2008 and July 2009 (Figure 5c). These may reflect uncertainties in the parameters relating to FC die-off and loading discussed previously, or the need for additional factors to be incrementally incorporated into the FC model to determine whether this allows for more nuanced simulation of FC loads. For example, a channel store where FC can be deposited, subjected to die-off and then re-suspended (e.g. Wilkinson et al., 2011) may contribute to reducing the over-estimation of FC loads in late 2008, whilst allowing for regrowth of FC in warmer temperatures (e.g. Cho et al., 2016b) may increase simulated FC loads in July 2009. As highlighted in Section 4.4, however, it is probable that many of these deviations are simply related to instances when the tracer-aided hydrological component of the model failed to capture subtleties in the observed discharge and isotope data (Figure 5). This was likely a consequence of the lumped structure of the semi-distributed model not being able to capture the drivers of subtle non-linearities in the discharge response of the BB, such as the influence of micro-topography (e.g. Frei et al, 2010) and fill-and-spill mechanisms which establish transient connectivity between the stream and interconnected pools that often make up riparian peatland drainage networks (Lessels et al., 2016; Soulsby et al., 2015; Sprenger et al., 2017). The use of more spatially-distributed models would help overcome these issues, as well as enable sources of FC to be modelled as highly localised phenomena (e.g. individual deer faeces) whose connection to the stream will depend on the spatial distribution of active flow paths (c.f. Dymond et al., 2016).

5.2 Future prospects for combining FIO and tracer-aided hydrological modelling approaches

A prerequisite to using models in exploring hydrological controls on water quality is the realistic simulation of hydrological processes and internal catchment states to which water quality parameters
are sensitive (Vache and McDonnell, 2006). In this study, insight into hydrological process realism provided by the tracer-aided model component helped understand whether discrepancies between simulated and observed FC dynamics were indicative of a need to refine the hypothesis conceptualised within the FC component of the model, or if they may have arisen due to inadequacies in the simulation of hydrological processes. In this way, coupling of FIO and tracer-aided hydrological models clearly has promise for assessing how factors such as hydrological connectivity drive stream FIO dynamics. Here, we provide a “roadmap” for the future development and application of coupled FIO and tracer-aided models based on our experiences in this study.

Integration of stable isotope tracers into spatially-distributed models has been steadily increasing (e.g. Kuppel et al, 2018; Remondi et al., 2018; Stadnyk et al., 2013; van Huijgevoort et al., 2016). Such modelling approaches have been successful in capturing the spatial and temporal dynamics of discharge and stable isotope tracers, and also permit more specific interrogation of how different parts of the catchment contribute to runoff generation under varying hydrological conditions (Ala-aho et al., 2017; Kuppel et al., 2018; Remondi et al., 2018). In this way, such modelling approaches could help overcome some of the structural limitations of the model presented here. Furthermore, spatially-distributed modelling frameworks could also facilitate inclusion of particle-tracking (e.g. Davies et al., 2011) or agent-based strategies (e.g. Reaney, 2008) that can explicitly track water particles and their associated tracer and contaminant characteristics through catchments (Davies et al., 2013). There is potential for developing spatially-distributed modelling with isotopes, particularly with cheaper isotope analysis increasing the viability of conducting repeat synoptic sampling of tracers (e.g. Ala-aho et al., 2018; Lessels et al., 2016) that can be used in calibration or to test how well a model can simulate spatial variability in hydrological processes and tracer concentrations (Birkel and Soulsby, 2015). If combined with efforts to better characterise the spatial distribution of FIO inputs (e.g. with repeated field mapping or use of remote monitoring techniques such as cameras or GPS tags on animals), and synoptic surveys of stream FIO concentrations (which may be feasible using rapid enumeration techniques such as the IDEXX Coliert-18 method, which require very little sample processing time prior to incubation
[Kinzelman et al., 2005]), the coupling of FIO models to spatially-distributed tracer-aided models would likely be transformational in elucidating the role of connectivity in driving stream FIO dynamics.

An important comment relates to data. For the application of spatially-distributed coupled models, the collection of spatially-distributed data relating to FIO loading of the landscape and stream FIO concentrations will be necessary. However, more fundamental requirements for any FIO modelling exercise will, firstly, be the collection of data that can allow more certain characterisation of FIO loadings by wild animals and the associated die-off behaviour of such FIOs (Guber et al, 2015; Muirhead et al., 2011), particularly in relation to extreme conditions such as repeated freeze-thaw cycles experienced over winter. Secondly, there is also a need for means of collecting higher-temporal resolution stream FIO data to be developed. Whilst the weekly data used in this study are informative, data that can resolve shorter-timescale variability in FIO dynamics will help to fully decipher how hydrological processes and microbial water quality are linked (c.f. Kirchner et al., 2004). Standard time frames for the analysis of water samples for FIOs have dictated that the collection of longer-term, high-temporal resolution FIO data has so far only really been possible with intensive field campaigns that involve the collection and processing of grab samples on a daily basis (e.g. Kim et al., 2017). However, with sufficient site-specific investigations on the impact of sample storage time on FIO concentrations, the use of autosamplers may help to ease the logistical burden of collecting longer-term, high-frequency FIO datasets (e.g. Hathaway et al., 2014; Oliver et al., 2015). In addition, there are also emerging technologies that can monitor beta-D-glucuronidase enzymatic activity in streams in near real-time, which may have potential to provide high temporal-resolution data relating to microbial contamination that can complement more traditional means of FIO enumeration (Stadler et al., 2016; Ender et al., 2017). Exploiting these advances in the collection of higher frequency data is likely to be instrumental in permitting a more thorough evaluation of hypothesised linkages between hydrological connectivity and FIO dynamics (de Brauwere et al., 2014; Oliver et al., 2016).
Finally, whilst this study has been based at a well-researched, data-rich, temperate site, it should be noted that future applications of coupled FIO and tracer-aided models need not be limited to such locations. For example, previous studies in more data-sparse tropical and karst regions have successfully used shorter-term or event-based tracer data to test and constrain multiple model structures as competing hypotheses of catchment hydrological functioning, despite the potentially greater complexity of hydrological processes operating in such landscapes (Birkel and Soulsby, 2016; Westerberg and Birkel, 2015; Zhang et al., 2017; 2018). As such, there is clear scope for employing coupled modelling approaches in such regions to explore controls on FIO dynamics; indeed, improved FIO modelling approaches in karst systems has been identified as a key research priority, in particular (Buckerfield et al., 2019). In addition, whilst data-rich catchments offer an obvious test-bed for developing new modelling approaches (Tetzlaff et al., 2017), the process understanding gained especially through the application of parsimonious models is likely to be somewhat transferable to similar catchments that have less data availability or are ungauged (c.f. McDonnell et al., 2007). Therefore, insights from parsimonious coupled modelling approaches into the controls on FIO dynamics in data-rich catchments are likely to still be informative for the management of microbial water quality more generally.

Conclusions

In this study, we have provided a “proof-of-concept” with respect to how tracer-aided hydrological models can be used to explore linkages between hydrological processes and microbial water quality. Specifically, we used a simple FC model coupled to a tracer-aided model to assess the hypothesis that hydrological connectivity between landscape units and the stream in northern upland catchments exerts a dominant control on stream FC dynamics by facilitating runoff-driven FC fluxes. The skill of the tracer-aided model component in simulating the general dynamics of observed discharge and isotope data provided confidence in the realism of the hydrological processes simulated by the model. As such, the ability of the model to simulate weekly observed FC loads at certain times of the year inferred that hydrological connectivity is likely a dominant control on stream FC dynamics during these periods.
particular, the crucial role of hillslope connectivity to the riparian zone during summer to provide FC for mobilisation to the stream despite reduced fresh inputs from red deer due to seasonal movements, was highlighted. Failure of the model to simulate lower winter FC loads could have reflected limitations in the data available for driving the FC component of the model. However, the specific timing of model failure more likely indicated a need to refine the hypothesis conceptualised within the FC model, potentially to incorporate the impact of freeze-thaw cycles on FC mortality or a dilution effect of hillslope connectivity in winter. Other deviations between observed and simulated FC loads could highlight the need for additional processes to be incrementally incorporated into the FC model to assess whether they allow for more nuanced simulation of FC loads, but most probably reflected limitations arising from the lumped structure of the model.

The greater potential for evaluating hydrological process consistency afforded by the use of a tracer-aided model was valuable in assessing whether refinements to the hypothesis conceptualised within the FC model component may be necessary for more successful simulation of observed FC data, or if inadequate hydrological process representation may have resulted in deviations between observations and simulations. As such, coupling FIO and tracer-aided hydrological models has great potential in better understanding the drivers of stream FIO dynamics, particularly if models are applied to test hypotheses which are refined based on model successes and failures, and as new data become available. This will likely have significant value for the effective management of microbial water quality in a range of environments, especially if some of the opportunities for model development and data collection highlighted from our experiences in this study can be realised.

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Declarations of Interest: None
References


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Figure 1: The Bruntland Burn catchment showing a) Topography, extent of dynamic saturated riparian zone and location of stream monitoring; b) Main soil classes.

Figure 2: Conceptual diagrams of: a) The tracer-aided hydrological model. Variables in red are model inputs (P = precipitation; PET = potential evapotranspiration; dSat = daily saturation extent); black represents hydrological dynamic storage (Sup, Sat, S_low) and processes (flux equations for Q_up, Q_sat, Q_low and R, AET = actual evapotranspiration); green relates to isotope tracer simulation (c = isotopic composition, frac_sat = fractionation in riparian zone, MV = mixing volume); blue are parameters to be calibrated (a, b, r, k, α = rate parameters, α_ET = isotopic depletion factor); upSp, satSp, lowSp = mixing volumes). b) The faecal coliform (FC) model. Purple variables are defined randomly at each time-step (Deer In Catchment = binary variable to determine if deer are present or not, Total Deer = total number of deer in catchment if present, Excretion = load of FC excreted per deer per day). For the hillslope (up)
and riparian zone (sat), the variables deer, FCProd, FC, dieOff and FC_Flux are: number of deer in
source area as determined by the seasonal probability function, FC load added to storage, FC storage,
die-off from storage (calculated using Eq. 3), and FC Flux from hillslope to riparian zone and riparian
zone to the stream. $Q_{up}$ and $Q_{sat}$ are simulated runoff from the dynamic hillslope and dynamic riparian
zone, and $\text{max}Q_{obs}$ is the maximum observed discharge for the study period. The “min” function is used
in calculating FC fluxes to ensure that FC is not created if the model simulates runoff that exceeds the
maximum observed discharge.

Figure 3: Time series of a) Precipitation and stream discharge; b) Air temperature and potential
evapotranspiration (PET); c) Isotopic composition of stream water and precipitation (symbol sizes
proportional to precipitation amount); d) Stream faecal coliform (FC) concentrations (Conc.) and loads
– concentrations below the limit of detection (LOD) are plotted in red at the LOD (1 CFU 100ml$^{-1}$),
with the upper limits of associated loads calculated using the LOD as the concentration.

Figure 4: Time series of a) Precipitation, and of median simulated model outputs for b) Stream
discharge, groundwater and instantaneous contributions of the hillslope and riparian zone to water
available for evapotranspiration and runoff generation from the riparian zone; c) Stream faecal coliform
(FC) load and instantaneous contributions of the hillslope and riparian zone to FC available for
mobilisation from the riparian zone; d) Total FC stored in the catchment and distribution between the
hillslope and riparian zone at the end of a given timestep.
Figure 5: Time series of a) Observed and modelled stream discharge; b) Observed and modelled stream water isotopic composition; c) Observed and modelled stream faecal coliform (FC) loads. When an observed concentration (conc.) was below the limit of detection (LOD), an upper limit for the associated FC load (+) was calculated using 1 CFU 100 ml$^{-1}$ as the concentration. Log$_{10}(0)$ indicates periods when loads of FC were simulated to be 0 CFU day$^{-1}$. The blue shaded area in c) indicates the period potentially impacted by freeze-thaw cycles.

Tables

Table 1: Initial and calibrated ranges for the hydrological and isotope parameters of the model. Initial ranges for all parameters were informed by Birkel et al. (2010; 2015), with the exception of $\alpha_{ET}$ taken from Benettin et al. (2017).

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<tr>
<td>b</td>
<td>day$^{-1}$</td>
<td>[0.0001, 0.1]</td>
<td>0.036 [0.0028, 0.088]</td>
</tr>
<tr>
<td>r</td>
<td>day$^{-1}$</td>
<td>[0.2, 0.9]</td>
<td>0.60 [0.28, 0.87]</td>
</tr>
<tr>
<td>k</td>
<td>day$^{-1}$</td>
<td>[0.001, 0.1]</td>
<td>0.053 [0.014, 0.095]</td>
</tr>
<tr>
<td>$\alpha$</td>
<td>-</td>
<td>[0.1, 0.9]</td>
<td>0.55 [0.27, 0.85]</td>
</tr>
<tr>
<td><strong>Isotopes</strong></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>upS$_p$</td>
<td>mm</td>
<td>[0, 1000]</td>
<td>363 [136, 721]</td>
</tr>
<tr>
<td>satS$_p$</td>
<td>mm</td>
<td>[0, 1000]</td>
<td>88 [12, 237]</td>
</tr>
<tr>
<td>lowS$_p$</td>
<td>mm</td>
<td>[0, 1000]</td>
<td>534 [64, 952]</td>
</tr>
</tbody>
</table>
\[ \alpha_{ET} \quad - \quad [0.95, 1.0] \quad 0.97 [0.95, 0.99] \]

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1174 **Declarations of Interest:** None

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1176 **Author Contributions:** AJN adapted a tracer-aided hydrological model developed in earlier work led by DT and CS, and coupled this to a faecal coliform model written by AJN with input from all co-authors. Data collection for use in model calibration was led by DT and CS. All authors were involved in data and model interpretation. AJN prepared the manuscript with contributions from all co-authors. All authors have approved the final manuscript.

1181

1182 **Highlights**

1183

1184 • Couple faecal coliform (FC) and tracer-aided models to explore drivers of FC loads

1185

1186 • Good simulation of discharge and isotopes indicates hydrological process realism

1187

1188 • Connectivity sustains stores of FC available for transfer to the stream in summer

1189

1190 • Freeze-thaw cycles or a hillslope connectivity dilution effect may be key in winter

1191

1192 • Spatially-distributed models and enhanced FIO data collection are useful next steps
a)  
\[ P_{up} = P \ast (1 - d_{Sat}) \]
\[ \text{PET}_{up} = \text{PET} \ast (1 - d_{Sat}) \]

\[ AET_{sat} \]
\[ \frac{c}{\text{sat}} \]
\[ \text{frac}_{sat} \text{ (Eq. 2 \( \alpha_{ET} \))} \]

\[ Q_{up} = a \ast S_{up} \]
\[ c_{Q_{up}} = Q_{up} \ast c_{up} \]

\[ S_{sat} \]
\[ \text{satMV} = \text{satS}_{p} \ast d_{Sat} \]

\[ Q_{sat} = k \ast S_{sat}^{1+\alpha} \]
\[ c_{Q_{sat}} = Q_{sat} \ast c_{sat} \]

\[ Q_{stream} = Q_{low} + Q_{sat} \]
\[ c_{Q_{stream}} = c_{Q_{low}} + c_{Q_{sat}} \]

Dynamic Hillslope

Recharge \( R = r \ast S_{up} \)
\[ cR = R \ast c_{up} \]

Dynamic Riparian Zone

Groundwater Reservoir

b)  
\[ \text{dieOff}_{Up} \text{ (Eq. 3)} \]

\[ \text{dieOff}_{Sat} \text{ (Eq. 3)} \]

Deer In Catchment

Total Deer

\[ \text{dieOff}_{Up} \]
\[ \text{dieOff}_{Sat} \]

\[ \text{upFCProd} = \text{deerUp} \ast \text{Excretion} \]
\[ \text{satFCProd} = \text{deerSat} \ast \text{Excretion} \]

\[ \text{upFC} \]

\[ \text{satFC} \]

Dynamic Hillslope

Dynamic Riparian Zone

\[ \text{upFC}\_\text{Flux} = \text{upFC} \ast \text{min}\{1, (Q_{up} \div \max Q_{obs})\} \]
\[ \text{satFC}\_\text{Flux} = \text{satFC} \ast \text{min}\{1, (Q_{sat} \div \max Q_{obs})\} \]

streamFC Load