

1 **Cleat structure analysis and permeability simulation of coal samples based on micro-computed**
2 **tomography (micro-CT) and scan electron microscopy (SEM) technology**

3 Alexandra Roslin^a, Dubravka Pokrajac^a, Yingfang Zhou^{a*}

4 ^a School of Engineering, University of Aberdeen, Aberdeen, AB243UE, United Kingdom

5 **Abstract**

6 Coal has been playing an important role as a valuable source of energy for many years. In turn, gas
7 production from coal reservoirs is a modern development and coal bed methane (CBM), also known
8 as coal seam gas (CSG), is attracting global attention due to its wide occurrence and benefits for the
9 environment as opposed to the conventional energy sources. Developing coal bed methane reservoirs
10 requires better understanding of the flow behaviours of gas and liquids in cleats and analysis of
11 possible contribution of pores to the flow. This paper describes the implementation of micro
12 computed tomography (micro-CT) and scan electron microscopy (SEM) techniques for analysis of coal
13 samples. Intermediate rank coal samples used in this study were collected from Southern **Qinshui**
14 **Basin (China)**. In the course of the described research, coal samples were scanned, processed and
15 segmented to study the cleat spacing and permeability. Due to the partial volume effect, the
16 resolution of cleats needed improvement which was achieved by subvoxel processing using a novel
17 algorithm as explained in detail in the paper. Permeability was obtained through simulation of one
18 phase flow using Lattice Boltzmann method (LBM). The results show that the simulated permeability
19 is comparable to the analytical approximation. The subvoxel processing has proved an effective
20 method of overcoming the partial volume effect for the low resolution micro-CT images.

21
22 **Key words**

23 Coal bed methane; Micro-CT; SEM; Subvoxel algorithm; Permeability; Lattice Boltzmann method

24 **1. Introduction**

25 Coal seam gas (CSG), also known as coal bed methane (CBM), is a form of unconventional natural gas
26 extracted from coal reservoirs. Unconventional resources are those hydrocarbon reservoirs whose
27 permeability/viscosity ratio requires use of technology to alter either the rock permeability or the fluid
28 **viscosity, or both, in order to produce them at commercially competitive rates**. Unlike conventional
29 clastic deposits, coal seams contain a high proportion of mostly localised organic matters in addition

30 to inorganic material. This results in dual-pore system where pores in organic matter are often too
31 small to be efficient flow paths, whereas much larger fractures (known as cleats) are believed to be
32 main conducts from which gas in organic matters can flow out (Clarkson and Bustin, 1996; Moore,
33 2012; Puri et al., 1991). Developing coal bed methane reservoirs demands better understanding of the
34 flow behaviour of gases and liquids in pores and fractures. This may require the use of sub-micron
35 resolution data for calculation of reservoir petrophysical properties and simulation of gas/water flow
36 behaviour. In turn, the latter demands thorough comprehension of the pore space structure of rocks.
37 **Micro-computed tomography and scanning electron microscopy provide an effective source of**
38 **information on the internal structure of coal porous space.**

39 The evolution of modern micro-CT imaging **techniques is based** on three-dimensional reconstructions
40 from a series of two-dimensional projections taken at different angles: the sample is rotated and the
41 absorption of X-rays in different directions is recorded and used to produce a three-dimensional
42 representation of the rocks and fluids (Blunt et al., 2013). The main advantage of X –ray micro-
43 computed tomography is that it yields high-resolution three-dimensional images of solid opaque
44 objects quickly and non-destructively (Carlson et al., 2003). It is similar to medical CT scanning, but
45 carried out on a smaller scale and with greatly increased resolution (down to less than 1 micron is
46 possible) (Golab et al., 2013). Implementation of such imaging is of value in a variety of applications,
47 including examination of clastic (Golab et al., 2010; Knackstedt et al., 2010), fractured basement
48 (Knackstedt et al., 2013) and carbonate (Arns et al., 2005) **reservoir rocks**, as well as three-dimensional
49 studies of coal (Mazumder et al., 2006), paper (Roberts et al., 2003), biomaterials (Knackstedt et al.,
50 2006), bones (Zezabe et al., 2005), volcanic ash (Ersoy et al., 2010), materials for palaeontology (Long
51 et al., 2006), soil science, meteorites, and geotechnics (Ketcham and Carlson, 2001).

52 In synchrotrons, which were exploited for first micro-CT images of rocks, a bright monochromatic
53 beam of X-ray is shone through a small rock sample (Flannery et al., 1987). The now-standard
54 **approach for scanning** the pore space of rocks is to use a laboratory instrument, a micro-CT scanner,
55 which houses its own source of X-rays (Arns et al., 2007). The X-rays are polychromatic, and the beam
56 is not collimated – the image resolution is determined primarily by the proximity of the rock samples
57 to the source (Blunt et al., 2013). The intensity recorded for the pixels (2D) and results from
58 reconstruction for the voxels (3D) obtained in micro-CT analysis represents the relative radio density,
59 or relative attenuation of X-rays through individual segments of the imaged material (Novelline, 1997).
60 Within the tomogram, the X-ray opacity of the material in each individual segment determines its
61 brightness, allowing a three-dimensional image to be reconstructed from sections viewed at different
62 angles (Golab et al., 2013). Voids are usually represented as black in micro-CT images due to their low

63 X-ray opacity, minerals are usually light grey (or white) to medium grey due to intermediate X-ray
64 opacity (Golab et al., 2013).

65 Many researchers have exploited computed tomography for quantitative characterisation of fractures
66 in coal (e.g. Mazumder et al., 2006; Van Geet and Swennen, 2001 etc.). Other researchers used micro-
67 CT techniques to investigate gas **adsorption and desorption in coal** (e.g. Karachan and Okandan, 2001),
68 as well as to investigate the heterogeneity and spatial distribution of pores (Giffin et al., 2013),
69 fractures (Yao et al., 2009) and distribution of organic and mineral matter (e.g. Verhelst et al., 1996;
70 Simons et al., 1997) in coals of different rank. The behaviour of fluids in pore space of rocks was
71 extensively examined, but those research studies mostly concentrated on sandstones (Berea
72 sandstone etc.) and carbonates (for example, Estailades carbonate) (Blunt et al., 2013), with **only a**
73 **few focusing** on simulation of gas flow in porous space of coal (e.g. Jing et al., 2016).

74 In addition to 3D imaging methods, there are other methods, well established in two dimensions, for
75 producing very fine images of rock samples. Amongst them the most widely applied is SEM (scanning
76 electron microscopy) which produces images down to resolution of 10s nm (Blunt et al., 2013). SEM
77 is a technology which generates ultra-high resolution two-dimensional images of thin rock samples
78 (Lemmens et al., 2010). As opposed to micro-CT, this method is destructive, but its advantage is that
79 it allows revealing details of small pores which are beyond the resolution of micro-CT images. SEM
80 images are often **used to: provide details which are beyond the resolution of micro-CT images** (Golab
81 et al, 2013; Ramandi et al., 2016); calibrate micro-CT images (Mostaghimi et al., 2015); generate
82 synthetic 3D structures from two dimensional thin sections (Wu et al., 2006).

83 For the purpose of the research described in this paper, micro-CT techniques were used in conjunction
84 with electron **microscopy to obtain sufficiently detailed images of intermediate rank coal sample and**
85 **to segment the cleats of those images**. The studied samples are characterised by irregular cleat system
86 which contains mainly thin, **poorly resolved fractures due to the partial volume effect**. The subvoxel
87 processing algorithm was applied in order to overcome that effect and to improve the quality of the
88 images. The subvoxelled images were then segmented and used for simulating of single-phase flow
89 through the pore space of coal samples. The idea of the subvoxel algorithm was taken from the
90 medical study of trabecular bones (Hwang and Wehrli, 2002) but the algorithm was written for coal
91 and it has never **previously been used for rock sample micro-CT images. The study described in this**
92 **paper concentrated on mm-scale effects**. Upscaling of these results to the larger scales was the
93 objective of a follow-up study.

94 2. Samples and samples preparation

95 Samples of intermediate rank coal from Panlong mine in Southern Qinshui coal bed methane basin
96 (China) were obtained and examined, the samples are buried in a range of 600-750 meters subsurface
97 and in this work one sample (Figure 1) was chosen in order to analyse cleat porosity and permeability.
98 The main characteristics of the analysed coal sample acquired from coal proximate analysis are listed
99 in Table 1.

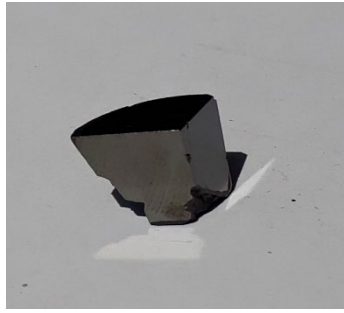


100
101 Figure 1. Coal core sample in a sample holder used in this study.

102
103 Table 1. Coal sample characteristics.

Sample ID	Sample (%)			Organic matter (%)			Vitrinite Reflectance ^o _{ran} (%)
	Organic matter	Pyrite	Others	Vitrinite	Inertinite	Liptinite	
PL3#-2	79.87	0.17	19.97	77.52	22.48	0.00	1.68

104
105 Previous studies (e.g. Wang et al., 2016; Cai et al., 2011) show that the coal from this basin contain
106 0.59 – 3.54% moisture, 3.5 – 15.54% ash yield, 73.62 – 88.92% fixed carbon and 2.14 – 4.04%
107 hydrogen, with C/H ratios in the range of 19.96 – 36.25. The vitrinite reflectance ranges from 1.95 to
108 3.49%, with 18.5 – 97.4% vitrinite and 2.4 – 81.4% inertinite. The gas in-place concentration is in the
109 range from 0.72 to 2.88x10⁸ m³/km², with an average of 1.21x10⁸ m³/km².
110 Samples were not dried or saturated with any high contrast fluid to preserve samples integrity. For
111 SEM analysis, the sample surface was polished in three different directions and carbon-coated (see
112 Figure 2).

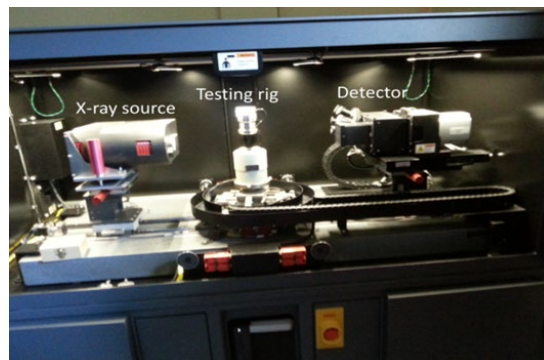


113
114

Figure 2. Coal core sample polished and carbon-coated for SEM analysis.

115 3. Methodology

116 X-ray micro-computed tomography was conducted using the laboratory-based ZEISS VersaXRM-410
117 3D microscope (Figure 3), which delivers non-destructive 3D imaging with submicron resolution, for
118 in situ scanning, and provides high-resolution micro-CT images for the widest range of sample sizes.
119 This machine uses patented detectors which convert X-rays into visible light and then uses a
120 microscope turret of objectives for easy and accurate zooming. VersaXRM-410 achieves 0.9 μm true
121 spatial resolution with minimum achievable voxel size of 100 nm. Advanced absorption and phase
122 contrast (for soft or low-Z materials) provide greater versatility in overcoming the limitations of
123 traditional computed tomography (CT).



124
125
126

Figure 3. ZEISS XRadia 410 Versa microscope (Kartal et al., 2017).

127 The first scan was done at the resolution of 25 microns to understand the internal structure of coal.
128 This scan was run at an X-ray beam energy of 80 kV and a power of 10 W. The distance between the
129 specimen and X-ray source was 57.024 mm while there was 97.76 mm between the specimen and
130 detector. An optical magnification of 0.4X was used to achieve high resolution. This gave a 25-micron
131 pixel size and exposure time was set to 1.2 s in order to get intensity values for the best signal-to-noise
132 ratio for each projection (radiograph). The next scan was done to achieve the resolution of 10 micron
133 to focus on the most vitrinite half of the sample. The scan parameters for all samples are summarised

134 in the Table 2. Having analysed 25- and 10-micron slides, the areas of interest were chosen, and four
135 2.5-micron slides were chosen with the most representative volume for porosity analysis and flow
136 simulation.

137 Table 2. Micro-CT scanning parameters.

Sample	Resolution, micron	Voltage, kV	Power, W	Distance to source, mm	Distance to detector, mm	Optical magnification	Exposure time, s
PL3#-2	25	80	10	57.0	97.8	0.4	1.2
PL3#-2	10	80	10	60.0	326.2	0.4	10
PL3#-2	2.5	120	10	65.0	110.0	4	15
PL3#-2	2.5	120	10	65.0	110.0	4	15
PL3#-2	2.5	120	10	65.0	110.0	4	15
PL3#-2	2.5	120	10	65.0	110.0	4	16

138
139 Scanning electron microscopy technique was also exploited during the research but only of the upper
140 surface of each sample at this stage. These SEM images were initially used for visual analysis of the
141 width, integrity and mineralisation of the fractures to understand which parts of the sample should
142 be targeted for scanning. Later, the samples were cut, and a few thin sections were prepared for
143 further SEM analysis. Because the thin sections were extracted from different parts of the samples
144 (not only from the surface) there will be an opportunity to calibrate micro-CT images with SEM data.
145 The SEM images were obtained with magnification 22, 27 or 29, 100, 150, 250, 300 and 350 depending
146 on the samples and the size of the features to be evaluated.

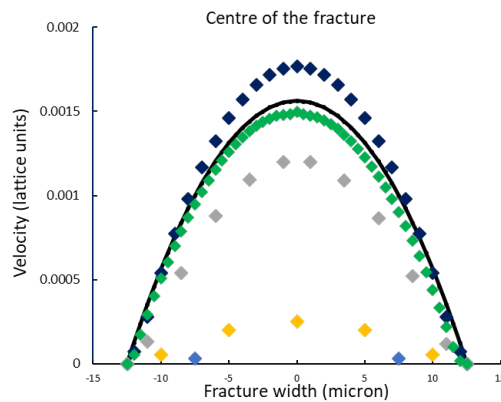
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148 4. Results

149 Grid independence test

150 Prior to calculating permeability of coal samples a grid independence test was carried out to validate
151 the simulation method, and to find the best resolution for a sufficiently accurate numerical simulation.
152 The test compared measured flow through a single fracture with constant width (defined by the
153 average fracture width in the studied sample determined from 2.5-micron scanned and 2.5-micron
154 subvoxelled images) to the analytical solution. The fracture width was 25 microns, and the simulations
155 were run for the following resolutions of the numerical grid: 2, 5, 10, 25 and 50 cells per fracture width
156 (i.e. 12.5, 5, 2.5, 1 and 0.5 micron cell size, respectively). The comparison of the velocity profiles across
157 the fracture with analytical solution is shown in Figure 4. It was observed that for resolutions coarser
158 than 10 cells per fracture width, there was a big discrepancy between analytical and numerical

159 solutions. At the same time, the most accurate resolution was 50 cells per fracture width, as expected
160 (Figure 4). Resolutions 25 and 10 cells per fracture width show 15% and 18% discrepancy respectively,
161 which was considered sufficiently accurate for the purpose of the study.



162
163 Figure 4. Velocity profile across the fracture width: analytical solution (continuous black line) and
164 numerical solution for different grid resolution (coloured symbols): blue – 2 cells per fracture width;
165 yellow – 5 cells per fracture width; grey – 10 cells per fracture width; dark blue – 25 cells per fracture
166 width; green – 50 cells per fracture width.

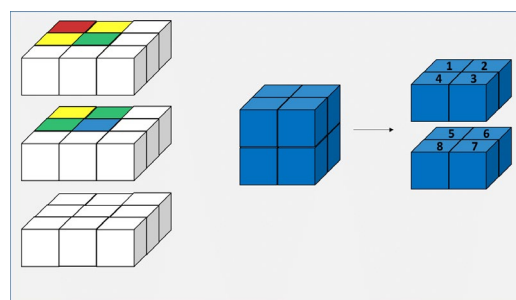
167
168 *Subvoxel processing and segmentation*

169 After micro-CT scans were obtained, images were processed and analysed versus SEM data, and it was
170 found that the resolution of cleats is quite poor due to the partial volume effect, and the width of the
171 cleats is overestimated for 25-, 10- and 5-micron scans compared to the width obtained from SEM
172 images (25 microns determined from SEM and 100 microns determined from 10-micron micro-CT
173 scans). On the other hand, the discrepancy between the widths of the cleats obtained from SEM and
174 2.5-micron micro-CT scans is about 1-2 micron. After couple unsuccessful attempts to improve the
175 resolution of cleats by application of different segmentation methods, the subvoxel processing
176 algorithm was written and implemented in Matlab to overcome the partial volume effect. After
177 analysis of SEM data and performing the grid dependence tests, we concluded that 2.5-micron
178 resolution appears to be the best solution for the studied samples. The problem of scanning samples
179 at 2.5-micron resolution is that the volume of investigation in case of this resolution is reduced to
180 2.5mm*2.5mm*2.5mm which was not sufficiently large to be representative. Collecting series of
181 separate volumes at 2.5-micron could have been a solution but it was difficult due to the scanning
182 time and expenses. Thus, it was decided to take 10-micron images and improve the resolution of these
183 images by subvoxel processing.

184 The idea to use subvoxel processing was taken from medicine (Hwang and Wehrli, 2002) and is
185 supposed to be applicable to volumes of interest containing materials or phases with two discrete

186 signal intensities (coal matrix and cleats in the case of current research). The principal strategy consists
187 of subdividing voxels and assigning voxel intensities to each subvoxel on the basis of local
188 neighbourhood criteria.

189 However, the approach to subvoxel processing was adapted and the algorithm was written to be
190 applicable for coal samples gray-scale images. Thus, the starting point of the algorithm for trabecular
191 bones images was the partitioning of each voxel into eight subvoxels by strictly enforcing conservation
192 of bone mass (Hwang and Wehrli, 2002). In order to ensure bone mass conservation, Hwang and
193 Wehrli (1999) generated bone volume fraction to determine the spatial distribution of trabecular
194 bone. In the current research, the subvoxel processing was performed directly on the gray-scale
195 images (where each voxel has a value from 0 to 255) and the restrictions to the algorithm were as
196 follows: 1) the average sum of eight subvoxels values should be equal to the value of the original voxel,
197 and 2) each subvoxel value could not exceed 255. Also, for trabecular bones images, each
198 neighbouring pixel had the same contribution but if the resulting subvoxel was next to the voxels with
199 zero BVF, **this subvoxel was zeroed. With the current research**, the following scheme was used: each
200 voxel was partitioned into eight voxels (1, 2, 3, ... 8 in Figure 5) and the resulting subvoxels were
201 assigned the gray-scale intensity values based on the intensity values of neighbouring voxels,
202 considering the proximity of each neighbour. Each subvoxel has 7 neighbours (for instance green,
203 yellow and red voxels shown in Figure 5 are the neighbours of the subvoxel 1): with 3 of them (green
204 in Figure 5) it has face-face connection, with 3 of them (yellow in Figure 5) – edge-edge connection
205 and with 1 of them (red in Figure 5) – point-point connection. The weight of each neighbouring voxel
206 is calculated based on the proximity to the subvoxel of interest: the weight of neighbouring voxels
207 with face-face connection is 25%, with edge-edge connection – 8% and with point-point connection –
208 1%. Subvoxel processing is an empirical algorithm rather than one derived from mathematical theory
209 (Hwang and Wehrli, 2002), so the optimal weighed contribution of each neighbouring voxel was
210 determined by trying different configurations and comparing the subvoxelled images to the images
211 scanned with higher resolution.

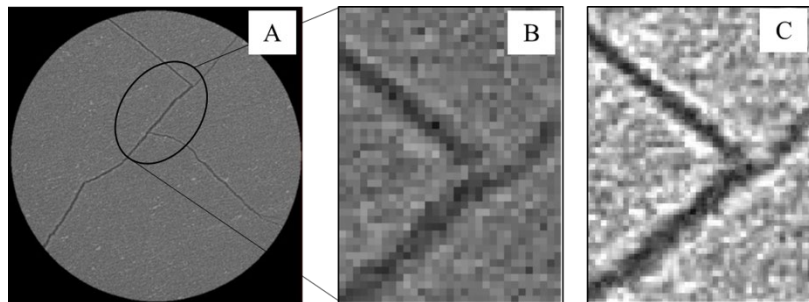


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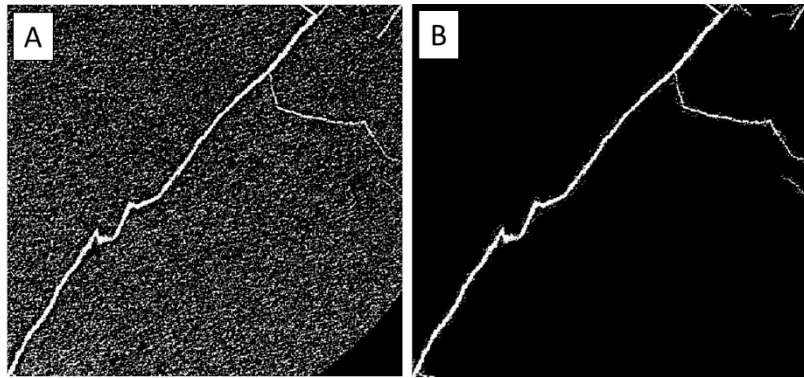
Figure 5. Subvoxel partitioning scheme in 3D.

214 For the purpose of this research, the same volume of coal sample was scanned with different
215 resolutions – 10-, 5- and 2.5-microns. Then, subvoxel processing was performed on 10-micron images
216 a couple of times with different weighed contribution of neighbouring pixels (starting from equal
217 weight of all neighbours and continuing towards an increase of contribution of face-face neighbours)
218 and after each iteration, the results were compared to the scanned 5-micron images, and when the
219 optimal result was achieved, subvoxel processing was repeated on subvoxelled images to achieve 2.5-
220 resolution. Then, the resulting 2.5-subvoxelled images were compared to scanned 2.5-micron images
221 for quality control. Images were compared in the following manner: the same features (similar
222 intervals of cleats) were chosen on 5- and 2.5-micron scanned image and the width of cleats was
223 determined by comparison with the one determined from SEM images. This calibrated width was
224 then compared to the width of the same features obtained from 5- and 2.5-micron subvoxelled
225 images. The results of subvoxel processing was accepted as optimal when the discrepancy between
226 the width of analysed cleats was about 1-2 micron (less than 10% of the width). As a result of
227 application of this method, the resolution of cleats was improved (Figure 6) but the volume of
228 investigation of new 2.5-micron subvoxelled images is 64 times bigger than that of 2.5-micron scanned
229 images.



230
231 Figure 6. An example of subvoxel processing results: A) 2.5-micron scanned image; B) 10-micron
232 image before processing; C) 10-micron image after processing to 2.5-micron subvoxelled image.

233
234 The next step of micro-CT scans analysis was image segmentation. Based on the experience of
235 previous researchers, the Ramandi et al., 2016 watershed method was chosen for image
236 segmentation. This approach was successfully applied by Ramandi et al. for Australian coal samples,
237 but used a combination of dry and wet coal images for better contrast between fractures and coal
238 matrix. In the course of the current research coal was not saturated with any contrast fluid, and as a
239 result of this, some unwanted noise appeared on segmented images which had to be removed by
240 different filters. The most effective filter for the studies samples was median filter (Figure 7).



241

242 Figure 7. The results of watershed- method segmentation in 2D and 3D – black is coal matrix, light

243

colour – cleat: A) before noise removal; B) after noise removal.

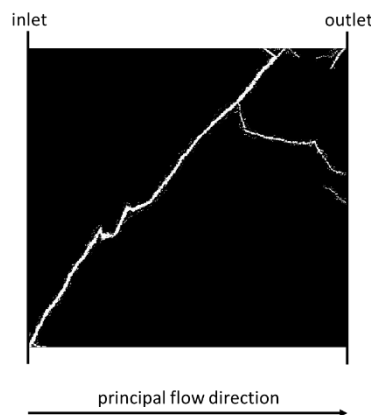
244

245 *Permeability simulation using LBM*

246

Permeability of coal samples was determined from numerical simulations of steady state single-phase flow through the samples. Simulations were performed using Palabos, which is an open-source computational fluid dynamics (CFD) solver based on the Lattice Boltzmann method. The Lattice Boltzmann method (LBM) is one of a number of particle-based CFD methods, where particles representing packets of fluid are tracked through the computational domain (Blunt et al., 2013).

250



251

252 Figure 8. An example of flow domain (2.5-micron scanned set) – the size of the sides is 2.5*2.5 mm.

253

254 Permeability simulation was performed on three different sets of images: 10-micron scanned, 2.5-
 255 micron scanned and 2.5-micron subvoxelled (Figure 8) to compare the results and estimate the
 256 sensitivity of permeability simulation to scanning resolution. For the simulation the following
 257 parameters were used: the D3Q19 lattice, bounce-back boundary conditions at the solid boundaries
 258 (walls), and a fixed pressure difference between the inlet and the outlet. A simulation starts with fluid
 259 having zero velocity, and with a constant pressure gradient in the x-direction (i.e. the principal flow
 260 direction). The permeability was computed by applying Darcy's law to the simulated velocity data,

261
$$k = U\mu \frac{dx}{dp} \quad (1)$$

262 here U is average velocity in x-direction in the cleat, μ is the fluid viscosity and $\frac{dp}{dx}$ is the pressure
 263 gradient along the principal flow direction (i.e. between the inlet and outlet).

264 Since reconstruction of 3D geometry can produce slightly different results depending on the value of
 265 threshold applied in the segmentation process, for each set of images listed above, permeability
 266 simulation was performed several times. Table 3 summarises simulated permeability results according
 267 to the different thresholds used in segmentation process: in the course of each image set
 268 segmentation, three different points on each intensity histogram were chosen for watershed
 269 segmentation, and the resulted images were used for simulation. To sum all, the following results
 270 were obtained: permeability was determined in the range 75-125mD for 2.5-micron subvoxelled
 271 images, in the range 125-205mD for 2.5-micron scanned images, in the range 2400-3000mD for 10-
 272 micron scanned images.

273 Table 3. Simulated permeability results depending on segmentation thresholds.

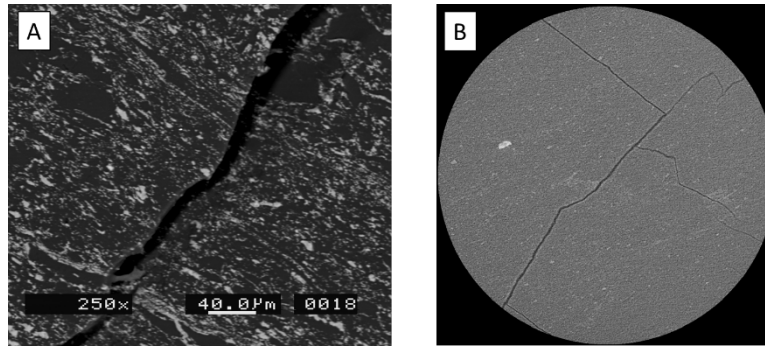
	Image set		
Threshold point on histogram	2.5 scanned	2.5 subvoxelled	10 scanned
25%	125 mD	75 mD	2400 mD
50%	152 mD	88 mD	2670 mD
75%	205 mD	125 mD	3000 mD

274

275 For the purpose of analytical solution, the fractures are assumed to have constant aperture d , to be
 276 parallel to the principal flow direction and to be at equal distances s , such that porosity of this system
 277 ϕ , is equal to the ratio d / s . Based on the analytical solution for Poiseuille flow between parallel plates
 278 the permeability of such system is:

279
$$k = \frac{\phi d^2}{12} \quad (2)$$

280 Previous researchers (e.g. Oron and Berkowitz, 1998) claimed that fracture aperture should be
 281 measured as an average over a certain length. Analysis of SEM and micro-CT images of the samples
 282 used in this research showed that coal fractures of studied samples are quite constant and consistent
 283 in width (see Figure 8), so it was decided to use average fracture aperture measured perpendicular to
 284 the main axis of fractures. Thus, analytical solution for the average fracture width (determined from
 285 2.5-micron scanned and 2.5-micron subvoxelled images) gave the value of 82.5mD which is
 286 comparable with numerical simulation results.



287

288 Figure 8. SEM image (A) and micro-CT image (B) demonstrate that the fracture width is quite
289 constant

290 5. Discussion, conclusion and future challenges

291 The research described in this paper focuses on implementation of micro-CT and SEM technologies
292 for analysis of coal including improvement of image resolution, and the sample from Southern Qinshui
293 Basin (China) was exploited for the research. It was observed that this coal was characterised by
294 irregular cleat system which contained mainly thin fractures. This had two consequences: 1) poor
295 resolution of those fractures due to the partial volume effect at lower resolutions (10- and 25-micron);
296 2) at higher resolution the scanned volume was too small to be representative of cleat system of those
297 samples. Taking into account these two considerations, it was decided to use subvoxel processing
298 algorithm to increase the resolution of 10-micron images to 2.5-micron but keeping volume of
299 investigation of 10-micron images. This method was proven on 10-micron images but also later tested
300 on different images with resolution from 25 to 2 microns. The idea for this approach was taken from
301 medicine, but the approach was adapted to the area of the research and the algorithm was written
302 based on the studied coal samples. The method was proved to overcome the partial volume effect, as
303 long as cleat width is larger than the pixel size of a scan. It was also observed that there is no value in
304 subvoxel processing below 2-micron resolution as it doesn't improve much the resolution of cleats.
305 The establishing of subvoxel algorithm was utterly important for the current research as this algorithm
306 allowed the authors to analyse coal thin features but significantly reduced the scanning time due to
307 bigger volume of investigation of each scan.

308 The problem of optimal resolution required for permeability simulation, which provides a good
309 balance between accuracy and efficiency, was also investigated in the course of this research. It was
310 found that the resolution that provides the most accurate permeability simulation (1.5% discrepancy
311 with analytical solution) is 50 cells per fracture, which equates to 0.5-micron resolution. The minimal
312 resolution for reasonably accurate simulation is 10 cells per fracture or 2.5 micron (18% discrepancy

313 with analytical solution). In the future, 2.5-micron resolution will be used as a standard to work with
314 these samples.

315 In the course of this research, the permeability simulation was also performed on different images
316 (with different resolution) and compared with analytical solution for Poiseuille flow in a single crack.
317 Permeability simulation was performed for two reasons: 1) it was required for validation of the results
318 of image subvoxelling and segmentation, and 2) the results obtained on mm-scale will further be used
319 to upscale permeability to cm-scale. Numerical simulation demonstrated that the permeability
320 simulated on 2.5-micron scanned images is in accordance with the permeability obtained for 2.5-
321 micron subvoxelled images (125-205mD and 75-125mD correspondingly), while 10-micron scanned
322 images gave the permeability in the range 2400-3000mD. Considering that the analytical solution for
323 an average fracture width gives permeability 82.5mD, it was concluded that simulation for 10-micron
324 scans greatly overestimated permeability. The latter supports the observation that the width of cleats
325 determined from 10-micron scanned images was also overestimated compared to the one obtained
326 from SEM data. However, the permeability obtained from the simulation is greater than the expected
327 from the analysis of coal samples from the studied coal basin. This was probably due to the scale
328 effect, i.e. to the fact that only a limited volume of coal was used for simulation. Moreover, this volume
329 contained a couple of fractures with considerable width, which increased the porosity of the sample
330 up to 4%. Analysis of the whole sample shows that the cleat porosity of the sample was lower (about
331 1.8%). Laboratory measurements of permeability of studied coal samples are in progress at the
332 moment but available data from the studied basin show that coal permeability is in the range 0.01-
333 0.37mD (Li et al., 2016).

334 The research described in this paper was performed at mm-scale and the problem of upscaling
335 permeability data to get permeability for the whole sample, as well as the validation of upscaling, is
336 not discussed in this paper. One possible way of addressing this challenge is to identify the key features
337 from rock images, e.g., self-similar behaviour (Wu, et al., 2019), which control the flow behaviour at
338 different scale and then apply the feature based approach (Singh and Cai, 2018a; 2018b) to estimate
339 the permeability at different scale. Finally, it must be noted that the research described in this paper
340 considered only cleat porosity and permeability. Pore matrix porosity will be investigated at the next
341 stage of the research.

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348

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